

3. You are given the following Python definitions:

```
a = 2
b = 3
c = 23.8
d = True
e = False
```

Evaluate the truth value of each Python expression below:

- `e or c > a`

- `(d and e) or (not d and not e)`

- `(a / b) > 0 and d`

- `((a * b) - 12) == 9`

4. Two trains a and b are on a collision course heading down the same track. If you know the speed of the two trains and how far apart they are, you can calculate when they will collide by the following formula:

$$collision = \frac{distance}{speed_a + speed_b}.$$

Write a Python program that asks the user for the speed of the two trains and their distance, calculates how long before the trains collide using the above formula, and prints the result to the screen. Be sure to include an informative message with the result, for example:

`Time until the trains collide: 3.862049.`

5. Hal wants to write a program that will tell him when to set his alarm clock. He has the input section already written, such that there is an integer variable for `day` according to 0=Sun, 1=Mon, 2=Tue, ..., 6=Sat, and a boolean variable `vacation` indicating if he is on vacation.

The program should print a string of the form 7:00 indicating when the alarm clock should ring. Normally, on weekdays (Monday through Friday) the alarm should print 7:00 and on the weekend (Saturday or Sunday) it should print 10:00. Unless he is on vacation—then on weekdays it should print 10:00 and weekends it should print `off`.

Below is shown Hal's first attempt; it is not correct.

- (a) Show **two specific** examples of values for `day` and `vacation` that cause the program to produce incorrect output.
- (b) Write a corrected version of the code.

```
if vacation and day > 5:
    print("off")
else:
    if day > 0 or day < 6:
        print("7:00")
    else:
        print("10:00")
```

6. Trace the execution of the following Python program in the template provided on the next page.

Showing your work (*e.g.* evaluation of expressions) is not required, but makes it much easier to give partial credit if you make a mistake.

```
i: int = 3
animal: str = 'cat'
if i < 1 or (animal == 'cat' and i > 1):
    i = i + 1
    animal = 'dog'
    print("yay")
elif animal == 'dog' and i > 1:
    i = i + 1
    animal = 'pig'
    print("boo")
if i > 5:
    i = i * 3
    print(animal)
else:
    i = i - 2
    print("no " + animal)
```

Scratch

Variables

Printed output

Extra practice

Distance bewteen two points

The shortest distance between two points is usually a straight line. However, the shortest distance between two locations on Earth is calculated with the great circle distance. Given two locations, this distance in kilometers is

$$6371.01 \operatorname{acos}(\sin(\phi_s) \sin(\phi_f) + \cos(\phi_s) \cos(\phi_f) \cos(\lambda_s - \lambda_f)),$$

where

- ϕ_s is the latitude of the starting point,
- λ_s is the longitude of the starting point,
- ϕ_f is the latitude of the final point, and
- λ_f is the longitude of the final point.

Write a program that asks the user for the latitude and longitude of two locations in decimal form, calculates the distance between them using the above formula, and prints the result to the screen.

Mercator projection

The Mercator Projection, formulated in 1569 by Gerardus Mercator, is the most commonly used 2D map projection of the globe and is seen on school walls across America. It has the property that compass bearings are accurately displayed, and is extremely useful for nautical purposes. Given a latitude ϕ and longitude λ , and using the Prime Meridian as the center of the map, we can find the x, y coordinate projection by:

$$x = \lambda$$
$$y = \frac{1}{2} \ln \left(\frac{1 + \sin(\phi)}{1 - \sin(\phi)} \right)$$

Write a Python program to prompt the user for input of floating-point numbers for phi (ϕ) and lambda (λ), perform the above calculations, and then display the corresponding x, y coordinates to the user. Note, \ln is the natural logarithm with base e .

Shoe sizes

European and American shoe sizes differ by a standard amount. You can approximate the European shoe size by using the following formulas.

For men:

$$euroSize = \frac{9}{7} americanSize + 30.5$$

For women:

$$euroSize = \frac{9}{7} americanSize + 29$$

Write a program that asks the user for the American shoe size and gender, calculates the European shoe size using the above formula, and prints the result to the screen.