

To get full credit for this homework assignment, it must be completed, but it will *not* be graded for correctness (unlike future homework assignments). Please answer the questions in simple, concise prose and when appropriate simple, concise pseudocode.

- What is your expected graduation year?
- What are your (intended) major(s) and minor(s)?
- How many times do you have to repeatedly halve 32 in order to reach 1? What about 8192? Consider the function which given an input n , outputs the number of times n can be repeatedly halved before falling below 1. What is the common mathematical name for this function?
- For each of the following, answer with the **best** (smallest) upper bound from this list: $O(\log n)$, $O(n)$, $O(n \log n)$, $O(n^2)$, $O(2^n)$.
 - number of leaves in a depth- n balanced binary tree
 - depth of an n -node balanced binary tree
 - number of edges in an n -node tree
 - worst-case run time to sort n items using merge sort
 - number of distinct subsets of a set of n items
 - number of bits needed to represent the number n
 - time to find the closest pair of points among n points in Euclidean space by simply listing all the pairs
 - time to insert n items into a binary heap
 - time to find the second largest number in a list of n (not necessarily sorted) numbers
- We will not use the syntax of any particular programming language in this course to specify algorithms. Instead, we will use well-written prose and pseudocode—an intuitive set of instructions that are appropriate to the problem at hand. For example, Algorithm ?? below gives some pseudocode for finding the smallest integer in an array.

Algorithm 1 FINDMIN(A, n)

Require: An array of integers A of length $n \geq 0$. Empty arrays return $+\infty$.

```

1:  $m \leftarrow +\infty$ 
2: for  $i \leftarrow 1$  to  $n$  do
3:    $m \leftarrow \min(m, A[i])$ 
4: end for
5: return  $m$ 

```

Write some pseudocode to find the smallest integer value in a binary tree T with left child $T.left$ and right child $T.right$ and integer value $T.value$. You can suppose that $T.left$ (respectively $T.right$) is NULL if it doesn't have a left (respectively right) child.

- Do you have any questions for me? If so, what are they?